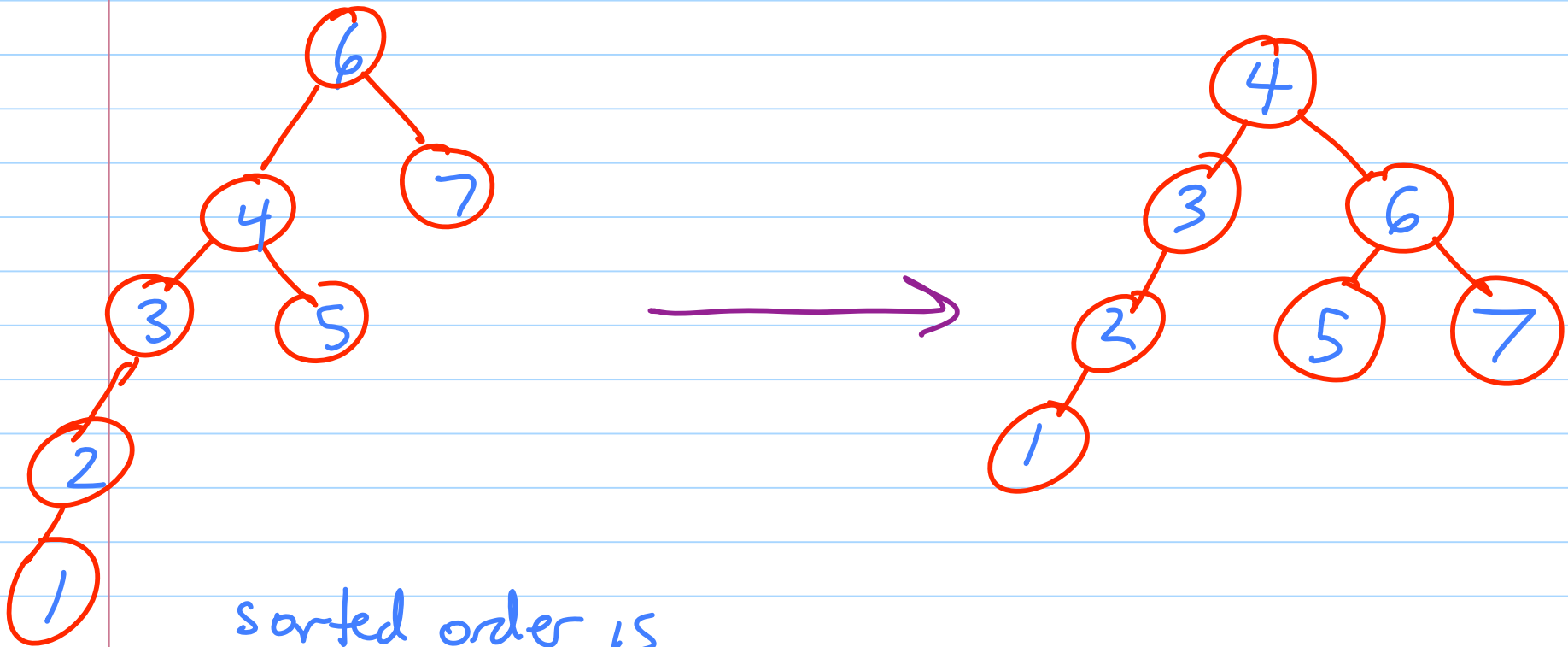


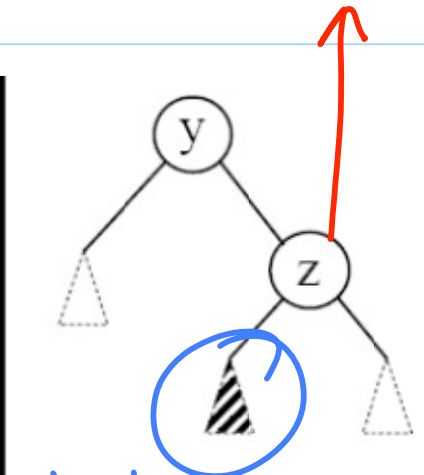
Balanced Binary Search Trees

Note Title

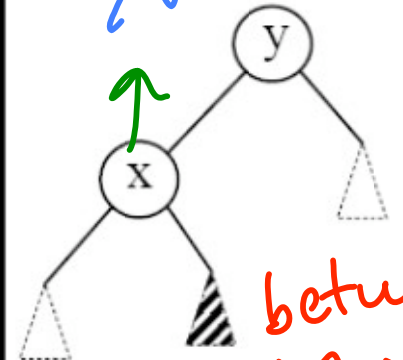
10/12/2007



sorted order is
given by an
in order traversal



between $y+z$

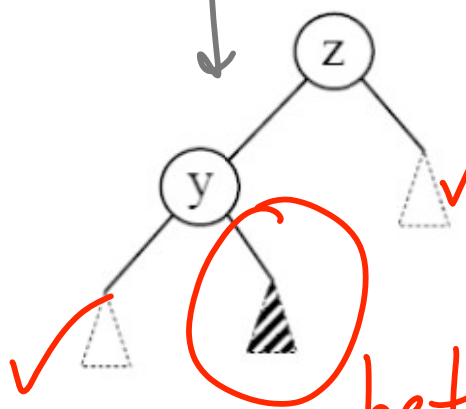


between $x+y$



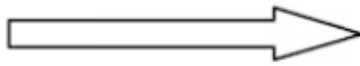
rotateLeft(y)

moves "weight" left

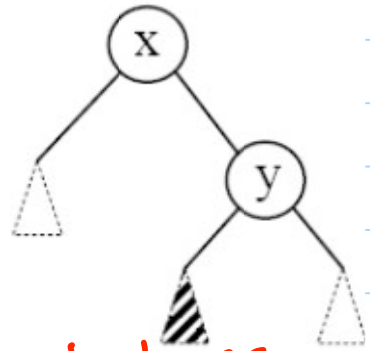


between $y+z$

$y+z$ change in their Parent/child relation
 + one subtree reattached



rotateRight(y)

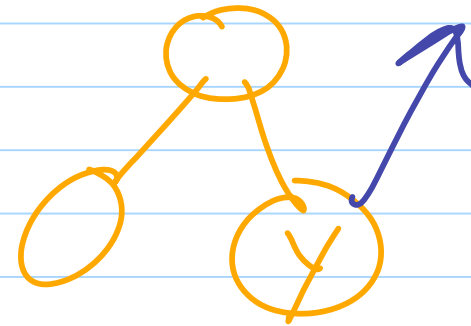
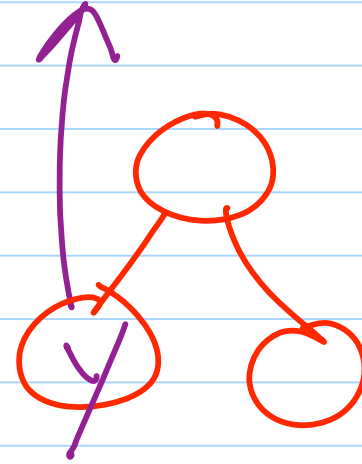


between $x+y$

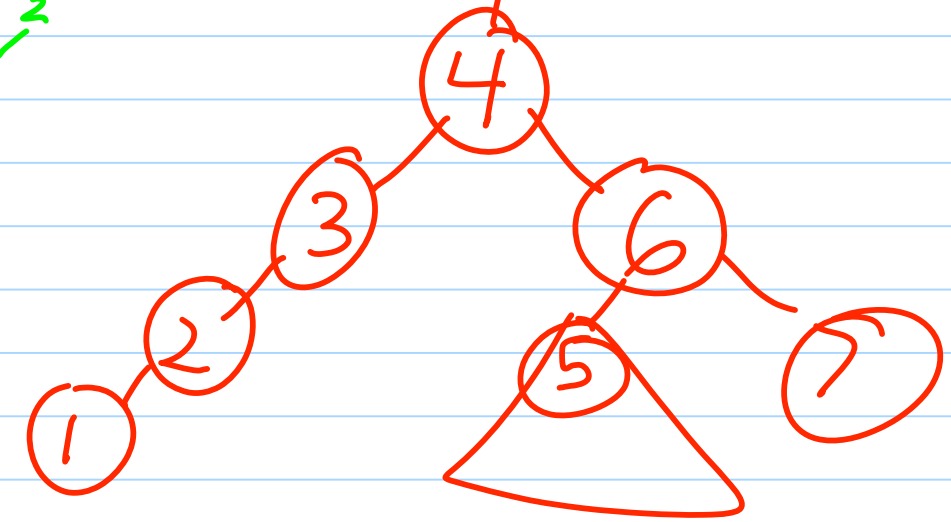
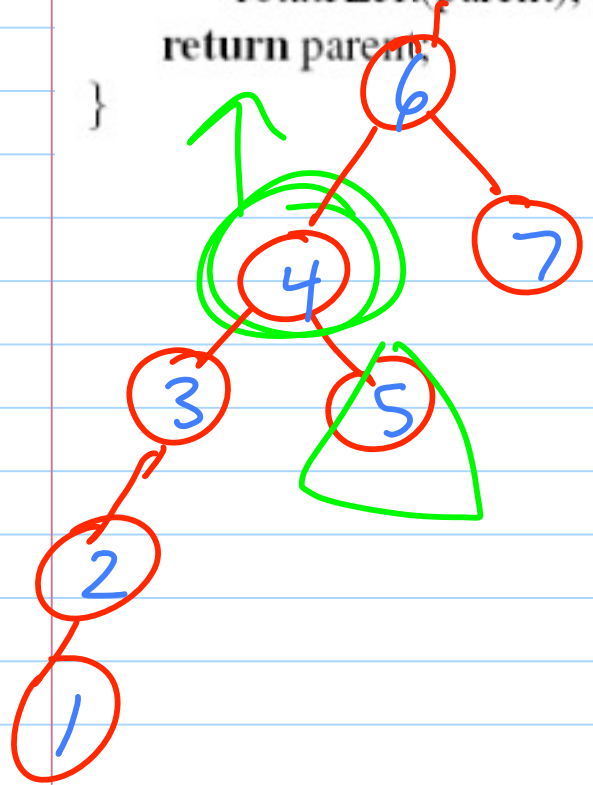
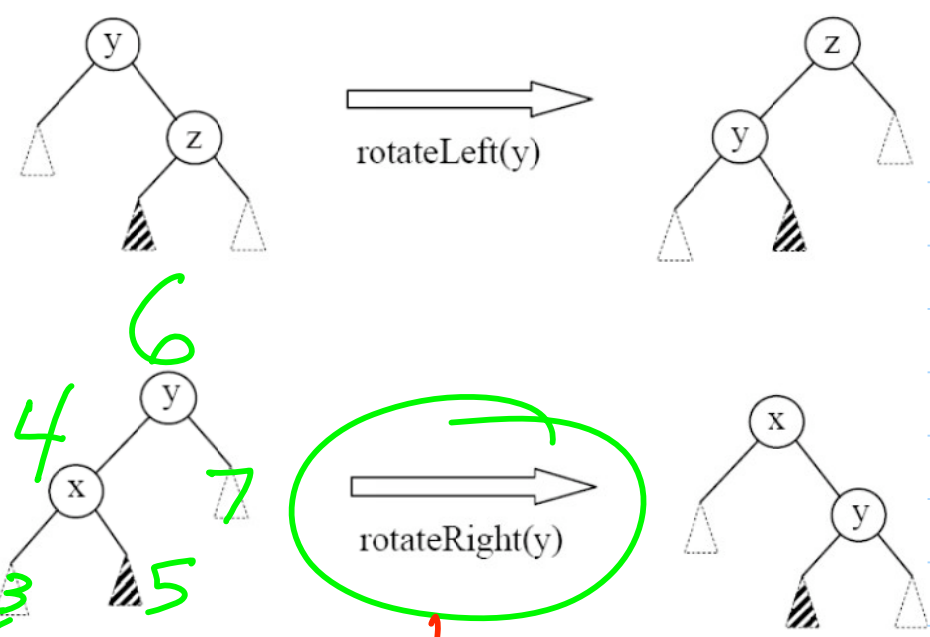
Requires parent is not null

internal

```
BSTNode liftUp(BSTNode y) {  
    BSTNode parent = y.parent;  
    if (y.isLeftChild())  
        rotateRight(parent);  
    else  
        rotateLeft(parent);  
    return parent;  
}
```



```
BSTNode liftUp(BSTNode y) {  
    BSTNode parent = y.parent;  
    if (y.isLeftChild())  
        rotateRight(parent);  
    else  
        rotateLeft(parent);  
    return parent;  
}
```



We can use rotations to help keep a binary search tree balanced while maintaining INORDER property.

Completely structural
(no new comparisons)

Difference between different data structures that are balanced binary search trees is how you decide when + where to rotate.

Red-black trees (after full break)
Guarantees height $\leq 2 \log_2(n+1)$

Book includes

Splay tree - amortized
rotates each element
accessed/insert to root

AVL trees - red-black trees
are a better choice